

## Properties of Exponents (review)

**Activity 1.** Fill in the gaps using the following words: power, base, exponent, degree, multiplied

An exponent (also called power or \_\_\_\_\_) tells us how many times the base will be \_\_\_\_\_ by itself.

For example  $x^5$  : the \_\_\_\_\_ is 5 and the \_\_\_\_\_ is x. This means that the variable x will be multiplied by itself 5 times. You can also think of this as 5 to the fifth \_\_\_\_\_ .

**Activity 2.** Complete the following list of properties of exponents:

Properties	General Form	Application	Example
<b>Product Rule</b> <i>Same base add exponents</i>	$a^m a^n$	$a^{m+n}$	$x^5 x^3 = x^{5+3} = x^8$
<b>Quotient Rule</b> <i>Same base subtract exponents</i>	$\frac{a^m}{a^n}$		$\frac{x^9}{x^5} = x^{9-5} = x^4$
<b>Power Rule I</b> <i>Power raised to a power multiply exponents.</i>	$(a^m)^n$		$(x^3)^4 = x^{3 \cdot 4} = x^{12}$
<b>Power Rule II</b> <i>Product to power distribute to each base</i>		$a^m b^m$	$(4x^3)^2 = 4^2 x^{3 \cdot 2} = 16x^6$
<b>Negative Exponent I</b> <i>Flip and change sign to positive</i>	$a^{-m}$		$x^{-3} = \frac{1}{x^3}$
<b>Negative Exponent II</b> <i>Flip and change sign to positive</i>	$\frac{1}{a^{-m}}$		$\frac{1}{x^{-5}} = x^5$
<b>Zero Exponent</b> <i>Anything to the zero power (except 0) is one</i>	$a^0$	$a^0 = 1$	$(-4x)^0 = 1$

It is important to note that none of these applications can occur if the bases are not the same.

For example,  $\frac{x^3}{y^4}$  cannot be simplified.

## Using a Combination of Rules

*At one point, you may be asked to use a combination of these properties.*

Example:

$$\bullet \frac{(2^3 y^2)^5}{2^{10} y^{16}} \quad \rightarrow \text{Power Rule}$$

$$\bullet \frac{2^{3 \cdot 5} y^{2 \cdot 5}}{2^{10} y^{16}}$$

$$\bullet \frac{2^{15} y^{10}}{2^{10} y^{16}} \quad \rightarrow \text{Quotient Rule}$$

$$\bullet 2^{15-10} y^{10-16}$$

$$\bullet 2^5 y^{-6} \quad \rightarrow \text{Negative Exponent}$$

$$\bullet \frac{32}{y^6}$$