CLIL Module Plan

| Author(s) | Ilaria Geat | ria Geat | | | | | | | | | |
|---------------|---------------------------|---|--|----------------|--|-----|------|--------|-----|--|--|
| School | Liceo Scientific | eo Scientifico "Leonardo da Vinci" Trento | | | | | | | | | |
| School Grade | O Primary | Primary O Middle | | | | | | | jh | | |
| School Year | 01 | 02 | | ● 3 ○ 4 | | | O 4 | | O 5 | | |
| Subject | Matematica | Matematica Topic | | | | | | circle | | | |
| CLIL Language | English | | | | | O D | euts | ch | | | |

Personal and social-cultural preconditions of all people involved

The scientific high school "Leonardo da Vinci" is one of the historical "Liceo" of the Province of Trento. Nowadays the "Leonardo da Vinci" high school proposes two curricula, foreseen by the reform of the high school: the ordinary scientific curriculum and the applied sciences scientific curriculum. The class consists of 20 Ss. There is a student of foreign origin, but perfectly integrated into the class; there are no SEN students; two Ss have lived for some years in an English- speaking country and therefore their English level is very high. The other Ss of the class present an average CEFR level B1+. Some Ss are particularly bright, some others do not study regularly. Although they have different mathematical competences, the average behavior is polite and participating and the class is generally collaborative. The Philosophy teacher has already started a CLIL experience. Therefore, the class has a certain idea of what a CLIL lesson should look like. The motivation and enthusiasm are high. The classroom is adequate to the number of Ss. The desks can be moved when needed for specific activities. A PC, an interactive whiteboard (IWB) and a whiteboard (WB) are available in the class. Ten laptops can also be used by the Ss (in pair work) if needed. The teacher (Ilaria Geat), who will carry out the CLIL Module, teaches Physics in this class and in seven other classes of the 1st and 2nd grade of the school, and she is the main teacher for this CLIL Module. She has a C1 English level certification and is planning Mathematics-CLIL Modules in collaboration with another colleague of her disciplinary Department. The Mathematics teacher in this class is Liliana Dal Bosco. Since her linguistic competences are not too high, she will not interact much in English during the lessons. However, she will listen (she understands English quite well) to Ss, observe Ss during each activity and, when needed, she will underline an important aspect in Italian.

Students' prior knowledge, skills, competencies

Subject

• Ss know basic properties of radicals and how to work with radicals. • Ss are able to solve a system of two second degree equations. • Ss have basic knowledge of analytic geometry. • Ss have already studied the straight line and the parabola.

Language

 The use of the following tenses is required: present simple and continuous, past simple, present perfect, future. • Modal verbs, the passive, the zero conditional, the first conditional and the second conditional will be used. • Ss know phrases and structures to make comparisons. • No subject-specific lexis is required. • Ss can understand the main concepts of a new video. • Ss have adequate reading skills. • Ss can take notes in English, while listening and simply answer open questions. • Ss can express an opinion in their own words.

Timetable fit

Module

Length 20 hours, 1 Unit, 11 Lessons

Description of teaching and learning strategies

• The learning and teaching objectives are disciplinary-specific, transversal and communicative. The lessons have been designed to encourage the development of problem solving, critical thinking, creative thoughts and ideas, collaboration, communication and time managing. • The methodological approaches will be various, in order to meet different learning styles and to promote the development of different skills: interactive lessons, group work (especially when the task is complex), pair work, individual work, TPS (Think, Pair, Share), cooperative learning. During the "student-centred" activities the teacher will act as facilitator and guide. • Interaction and communication will be promoted during the lessons as much as possible by the teacher, who will ask questions and invite Ss to comment or express their idea, and by group or pair works. During these activities, the teacher will circulate and model language, concepts and cognition. A quiz and two short competitions at the end of two lessons will contribute to promoting interaction as well. • As a ICT learning tool GeoGebra will be used both by the students during their pair work (using laptops) and by the teacher, sometimes in order to explore a new issue, some other times in order to verify hypotheses. Two online lessons available on YouTube will be watched in order to revise what previously learnt and also to introduce a new topic. • The teacher will provide different materials to support content and language scaffolding: a Glossary during the first lesson, that will help Ss developing the basic vocabulary necessary for this Module, various worksheets for the activities at school and exercises for homework in order to consolidate learning and practice. • During most activities a formative assessment by the teacher is provided and/or a peer- or self-evaluation is encouraged, while at the end of the Module a summative assessment is provided.

Overall Module Plan

Unit: 1

The circle

Unit length: 20

hours

Lesson 1

Definition and equation of the circle.

Lesson 2

Relation between the coefficients a, b, c in $x^2+y^2+ax+by+c=0$ and the graph of the circle.

Lesson 3

How to find the equation of a circle, giving some conditions.

Lesson 4

Intersections between a circle and a straight line.

Lesson 5

How to find the equation of a tangent line to a circle.

Lesson 6

Test to consolidate learning.

Lesson 7

Relative position of two circles.

Lesson 8

Families of circles.

Lesson 9

Subsets of the plane.

Lesson 10

A "complex" problem regarding the circle.

Lesson 11

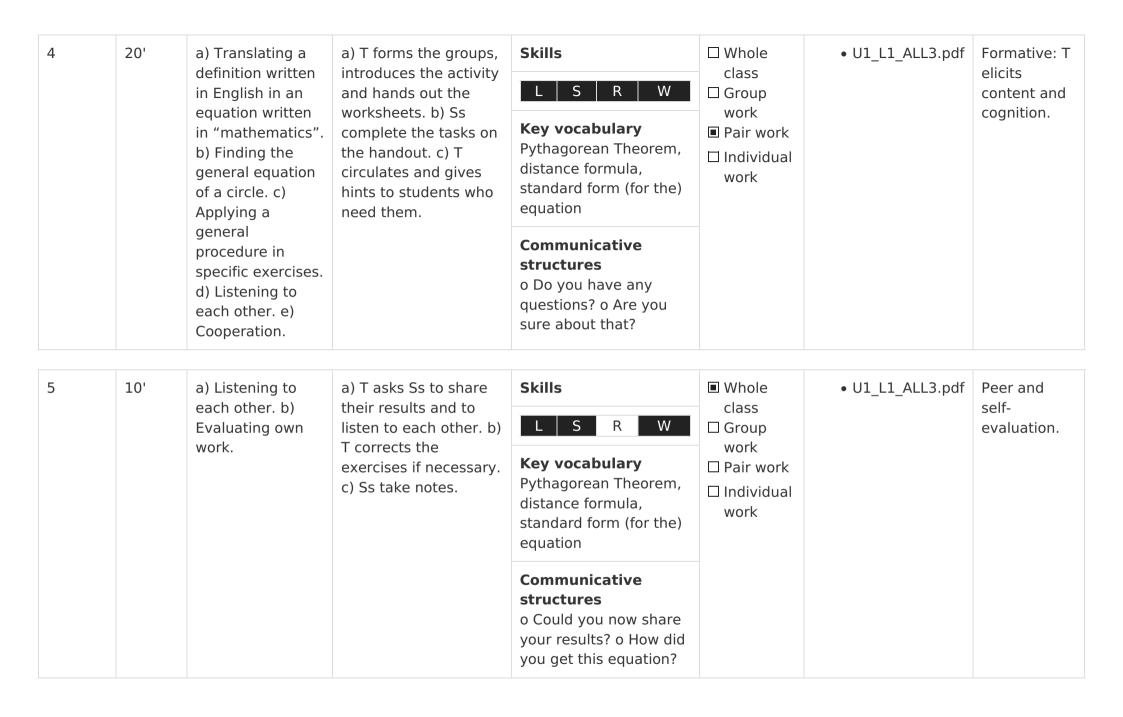
Final test.

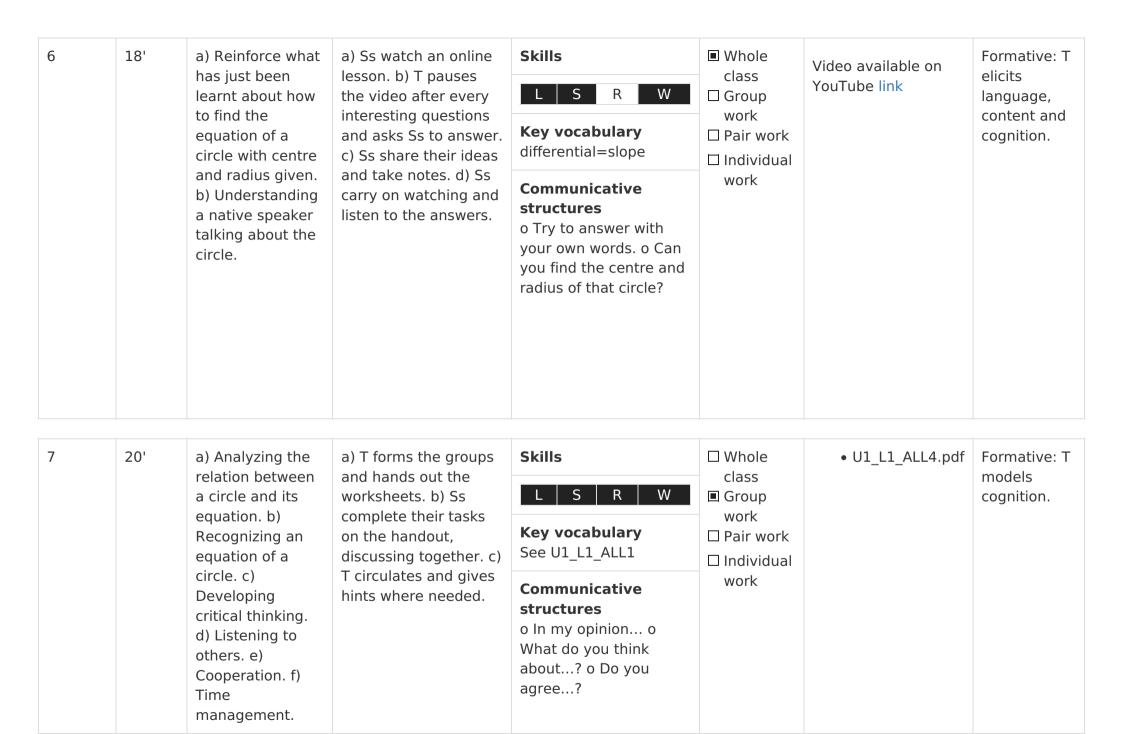
Unit number 1 Lesson number 1 Title Definition and equation of the circle.

| Activity | Timing | Learning Outcomes | Activity Procedure | Language | Interaction | Materials | Assessment |
|----------|--------|----------------------|--|---|--|-----------|------------|
| 1 | 5' | | a) T introduces and explains the aims, | Skills L S R W | ■ Whole class | | |
| | | | topic and objectives of the CLIL Module "The circle". b) T introduces the topic and learning outcomes of this first lesson. c) Students | Key vocabulary Circumference, circle, equation, intersection, graphs, straight line | ☐ Group work ☐ Pair work ☐ Individual work | | |
| | | | take notes. | Communicative structures • We are going to study • Our objective is • If you have any questions | | | |

| 2 | 10' | a) Building vocabulary and key words. b) Learning how to read "mathematics" in English. c) Cooperation. | a) T hands out the material and asks Ss to work in pairs. b) Ss complete the tasks on the handout. c) Each S writes two equations or mathematical expressions, reads them to his/her partner without showing him/her them and the partner writes them down. d) Ss exchange roles and then compare what they have written with the original equations or expressions. | Key vocabulary See U1_L1_ALL1 Communicative structures • My equation is: "x squared plus" • Could you please say that again? | □ Whole class □ Group work ■ Pair work □ Individual work | • U1_L1_ALL1.pdf | a) Formative:T models language then walks round, checks and facilitates. b) Peer assessment. |
|---|-----|---|--|---|--|------------------|--|
|---|-----|---|--|---|--|------------------|--|

| 3 | 7' | a) Formalizing a known concept | a) T hands out the material. b) Ss | Skills | ■ Whole class | • U1_L1_ALL2.pdf |
|---|----|--|--|---|--|--|
| | | (the circle) with a rigorous definition. | complete the tasks on the handout in small groups. c) Then, T asks Ss to share their definition in plenary | L S R W Key vocabulary Circle, distance, center, radius | ■ Group work □ Pair work □ Individual work | • A needle and a thread per group • WB |
| | | | and writes the right definition on the whiteboard. d) Ss take notes. | Communicative structures • Please, tell the class the definition of circle you have just written. • Do you think that's a good definition? • Do you have any suggestions to improve it? • Who has a different definition? | | |

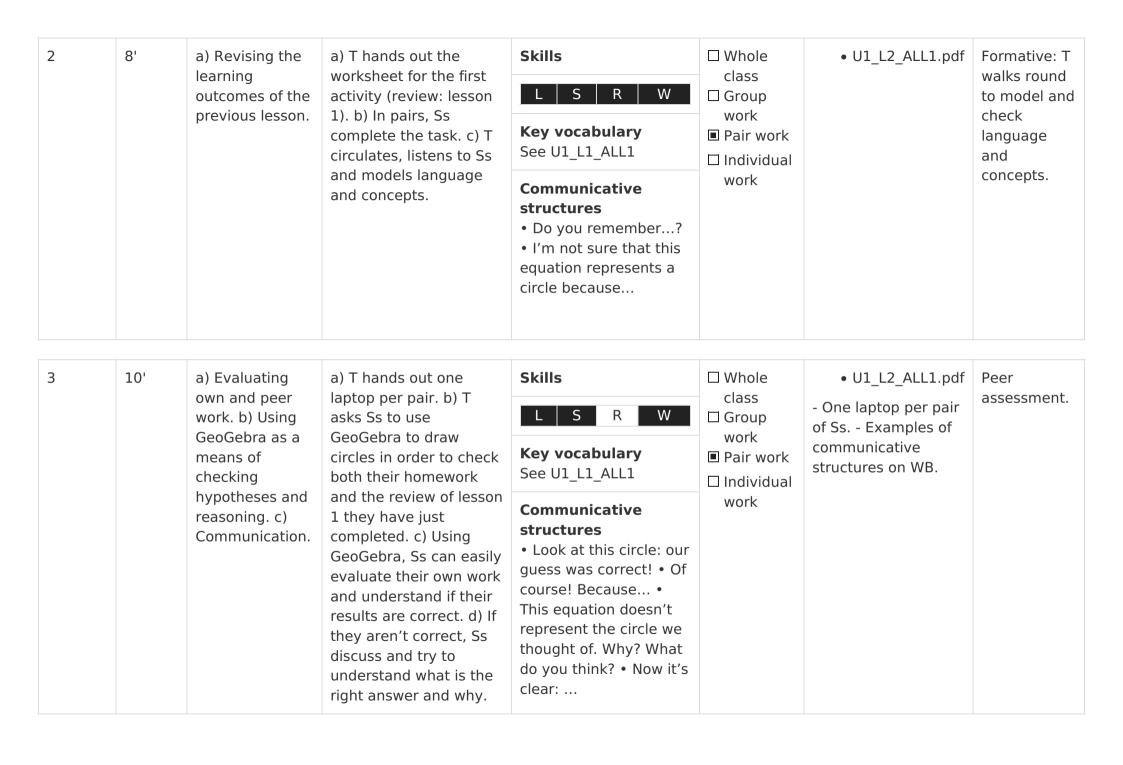




| 8 | 10' | a) Summarizing and formalizing. | a) Ss are asked to share their results of | Skills L S R W | ■ Whole class | • U1_L1_ALL4.pdf WB. |
|---|-----|---------------------------------|---|---|--------------------------|----------------------|
| | | b) Listening to others. | | | ☐ Group work | |
| | | | | Key vocabulary See U1_L1_ALL1 | ☐ Pair work ☐ Individual | |
| | | | lesson on the WB, Ss take notes. c) T gives Ss some more exercises for homework. For homework T also asks Ss to think about the connections between the sign of the parameters a, b in the general equation of a circle and the graph of the circle. This question will help to introduce the topic of the next lesson. | Communicative structures o What have you learnt today? o Could you please recall the definition of a circle? o Is it true that? o Do you agree if I say | work | |

Unit number 1 Lesson number 2 Title Relation between the coefficients a, b, c in x^2+y^2+ax+by+c=0 and the graph of the circle.

| Activity | Timing | Learning Outcomes | Activity Procedure | Language | Interaction | Materials | Assessment |
|----------|--------|----------------------|--|--|-------------------------------|-----------|------------|
| 1 | 5' | | a) T introduces the objective of the lesson | Skills | ■ Whole class | | |
| | | | and the activities. b) T | L S R W | ☐ Group | | |
| | | | explains the rules of the quiz Ss are going to do during the lesson. | Key vocabulary See U1_L1_ALL1 | work □ Pair work □ Individual | | |
| | | | | Communicative structures • Today we're going to • You're going to use GeoGebra in order to • At the end of the lesson there'll be a small prize for the winner of the quiz | work | | |



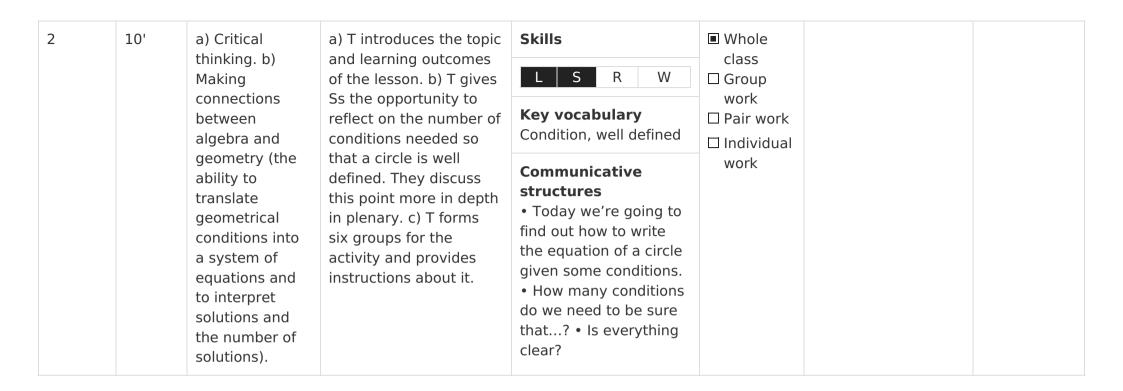
4 5' a) a) Going back to the Skills ☐ Whole Formative: T One laptop per pair Understanding question T gave Ss at class elicits of Ss. S R the relations the end of the previous W ☐ Group cognition. between the lesson about the work **Key vocabulary** coefficients a. b. meaning of the ■ Pair work Coefficients, sign c in the coefficients a. b. c in ☐ Individual (positive/negative) the standard form of equation of a work the equation of the circle and the Communicative circle. T asks Ss to use graph of the structures circle. b) Finding GeoGebra to explore • I think we could use this problem more a strategy for GeoGebra to draw using a deeply. b) Ss, who some circles with a technological should have already positive, then some tool (laptop, made a conjecture with a negative and about this problem at GeoGebra) in then we could home, should now think order to reach a compare... • In my to draw some circles specific goal. c) opinion if a is positive, Creative using GeoGebra with then..., because... • thinking. specific values for the And what happens coefficients a, b, c and when c is equal to zero? check if their • The coefficients a, b conjectures were right are related to the or not. (For example: if position of the centre... a is zero/positive/negative, then the centre lies...) c) Important: when T asks Ss to use GeoGebra in order to find the relations between a, b, c and the graph of a circle, T doesn't suggest how.

5 7' a) Time a) T briefly recalls the Skills ☐ Whole • U1 L2 ALL2.pdf managing. b) rules of the guiz: 1. The class S R Organizing the auiz consists of 10 W ☐ Group work (decide if it questions, 2. Ss should work **Key vocabulary** is faster to work find the answers to all ■ Pair work Coefficient, sign separately on questions in pairs and ☐ Individual (positive/negative), different then write them on an work centre sits on the x/v questions or to answer sheet and give axis, centre passes work together). it to T. 3. When the time through the origin, c) Cooperation. is over. T reads the quadrant d) Applying answers and gives the previous scores: 10 points for Communicative each right answer, -5 reasoning to a structures new specific for each incorrect How could we answer. 4. In case of a issue. e) organize work in the Understanding draw, the group that most efficient way? • I the relations has given the answer think it's fast to work between the sheet first is the winner. together... • I'm sure in b) T shows the 10 coefficients a, b, this circle b is equal to c in the questions on WB and zero. • I agree with you equation of a the guiz begins. c) Ss because this circle is work on the questions circle and the similar to the circle we graph of the as fast as they can, draw before using using what they have circle. GeoGebra... just understood during the previous activity with GeoGebra. d) Ss can organize the work as they prefer: they can divide the task and work separately on different questions or they can work together.

| 6 | 15' | a) Formalizing and generalizing. b) Evaluating own and peer work. c) Understanding the relations between the coefficients a, b, c in the | a) T reads the answers and writes them on WB together with the scores. b) T gives a symbolic prize to the winners. c) T discusses the results of the quiz with Ss and clarifies incorrect reasoning if necessary. d) T | Key vocabulary Coefficient, sign (positive/negative), centre sits on the x/y axis, centre passes through the origin, quadrant | ■ Whole class Group work Pair work Individual work | • U1_L2_ALL2.pdf • U1_L2_ALL3.pdf WB | Formative: • T keeps the answer sheets and assesses them. • Peer and self-assessment. |
|---|-----|--|--|--|--|--|---|
| | | equation of a circle and the graph of the circle. | formalizes what Ss have just discovered, drawing a diagram on the WB similar to the diagram in U1_L2_ALL3. e) Ss take notes and ask questions if necessary. | Communicative structures • And the winners are • You're right, because • Why did you write a=0 in circle n° 1? • In general, we could say that | | | |

Unit number 1 Lesson number 3 Title How to find the equation of a circle, giving some conditions.

| Activity | Timing | Learning Outcomes | Activity Procedure | Language | Interaction | Materials | Assessment |
|----------|--------|---|---|--|--|---------------------|--|
| 1 | 10' | a) Revising the learning outcomes of previous lesson. | a) In order to review the content of the previous lesson, T asks Ss to complete a task (review: lesson 2) individually. Then, if necessary, T corrects the homework on the WB. b) Ss complete their tasks individually and then ask questions about the homework. | Skills L S R W Key vocabulary See U1_L1_ALL1 Communicative structures • I'd like you to complete this review individually • Do you have any questions about the homework? | ■ Whole class □ Group work □ Pair work ■ Individual work | • U1_L3_ALL1.pdf WB | Formative: T collects the reviews and assesses them. |



| 3 | 20' | a) Problem solving: solving a new problem, using previous knowledge and the ability to make connections and | a) T hands out the material and asks each group to complete only one of the six tasks in U1_L2_ALL2 (T chooses which). Task n° 1 consists of two different tasks because these are | Skills L S R W Key vocabulary Condition, system, equation, parameter, solution | ☐ Whole class ☐ Group work ☐ Pair work ☐ Individual work | • U1_L3_ALL2.pdf | Formative: T models language, content and cognition. |
|---|-----|---|--|--|--|------------------|--|
| | | revise contents. b) Cooperation. c) Listening to others. | easier than the others. b) While Ss are working on their task, T circulates and facilitates if necessary. | Communicative structures • How could we translate this condition into an equation? • Do you agree? • Do you think there is an easier way to? | | | |

| 4 | 50' | a) Learning how | a) A student per group | Skills | ■ Whole | • U1_L3_ALL2.pdf | Formative: • T elicits |
|---|-----|--|---|--|------------------------------------|------------------|---|
| | | to write the equation of a circle, giving three conditions. b) Learning how to translate these | is asked to present the task they have worked | L S R W | class Group | WB. | language, content and cognition. • Peer reflection encouraged. |
| | | | on to the rest of the class and to complete it on the WB. b) Ss take notes and ask for clarifications if | Key vocabulary Condition, system, equation, parameter, solution | work □ Pair work □ Individual work | | |
| | | conditions into equations. c) Brushing up on previous knowledge about how to solve a system of equations. d) Find different ways to solve the same problem and compare them. | necessary. c) Where appropriate, T encourages peer-reflection on what groups have found and asks Ss questions to reflect on, in particular to think about different ways for solving the same problem. d) Task n° 6 has no solution. This is particularly interesting for the class. The student that presents this case is invited to discuss it and explain the reason why it seems to have no solution (the points A, B, P are aligned). | Communicative structures • How did you translate these conditions? • Do you think there is another way to find the equation of this circle? • Is it possible that no circle satisfies these three conditions? Why? | | | |

| 5 | 10' | a) Generalizing on reasoning and procedures done on a specific exercise and formalizing. | a) T formalizes and generalizes, drawing a table on the WB similar to the table in U1_L3_ALL3. b) Ss take notes. c) T gives Ss similar exercises for homework. | Skills L S R W Key vocabulary Condition, system, equation, parameter, solution | ■ Whole class Group work Pair work Individual work | • U1_L3_ALL3.pdf WB. |
|---|-----|--|--|--|--|----------------------|
| | | | | Communicative structures • In general we could • Formalizing • Given these three conditions • I'll give you these exercises for next time. | | |

Unit number 1 Lesson number 4 Title Intersections between a circle and a straight line.

| Activity | Timing | Learning Outcomes | Activity Procedure | Language | Interaction | Materials | Assessment |
|----------|--------|---|---|---|-------------------------------|-----------|------------|
| 1 | 10' | a) Revising the learning outcomes of previous lesson. | a) T, together with Ss, revises the topic of the previous | Skills L S R W | ■ Whole class | | |
| | | | lesson, giving some examples of conditions that a | Key vocabulary See U1_L1_ALL1 | work □ Pair work □ Individual | | |
| | | | circle satisfies and asking Ss to translate these conditions into a system of equations. b) T corrects the homework, if Ss have doubts. c) T introduces topic, objective and activities of this lesson. | Communicative structures • How would you translate the following conditions into a system of equations? • Today we're going to study the intersections between a circle and a straight line | work | | |

| 2 | 20' | a) Critical thinking. b) Communication. c) Cooperation. d) Making connections and comparisons. e) Finding analogies and differences between studied concepts. f) Understanding how many intersections a straight line and a circle can have. g) Classifying straight lines according to their intersections with a circle. h) Finding the intersections between a line and a circle both graphically and algebraically. | a) T hands out the worksheets for the first activity. b) Ss complete the task in pairs. c) T circulates to facilitate. | Key vocabulary Intersection, straight line, secant, tangent, external Communicative structures In my opinion It's clear that a line and a circle can't have three intersections. What about this case? I think that the definition should be modified because | □ Whole class □ Group work ■ Pair work □ Individual work | • U1_L4_ALL1.pdf | T collects the worksheets and assesses them. |
|---|-----|---|--|--|--|------------------|--|
|---|-----|---|--|--|--|------------------|--|

| 3 | 10' | a) Critical thinking.b) Communication.c) Justifyingchoices. d) Making | a) T asks Ss to share their results in plenary. b) T and Ss correct the task and | Skills L S R W | ■ Whole class □ Group work | • U1_L4_ALL1.pdf WB. | Formative: T models language and |
|---|---|---|---|--|-------------------------------|-------------------------|---|
| | () () () () () () () () () () | connections and comparisons. e) Finding analogies and differences between studied | discuss the main points, in particular T underlines that, in order to prove that the definition given | Key vocabulary Intersection, straight line, secant, tangent, external | □ Pair work □ Individual work | | cognition. |
| | | concepts. f) Finding the intersections between a lice and a circle both graphically and algebraically. g) Formulating a rigorous definition of a known concept. | for a tangent line to a circle could not work for a tangent line to a parabola, Ss need to find a counterexample. c) T insists on this point and asks Ss to formulate a definition of tangent line to a parabola. T guides Ss in formulating this definition and writes it on the WB. | Communicative structures • Would you share your ideas with the whole class? • Did you manage to find a counterexample? • What's the solution of the system? • Could you now formulate a definition that works for a straight line tangent to a parabola? | | | |

| 4 | 40' | a) Developing reasoning skills. b) Solving a new complex problem, "a real life" problem. c) Finding a suitable mathematical model for a "real life" problem. d) Translating a complex problem written in English into a problem written in "mathematics". e) Critical thinking. f) Creative thinking. g) Communication. | a) T forms the groups for the activity and hands out the worksheets. b) In this activity Ss are asked to solve a "complex" problem. They need to understand the problem, find an appropriate mathematical model that describes it and use this model to find a solution for the original problem. c) T circulates, listens to Ss and facilitates. | Key vocabulary Channel, underground, explosion, damaged area, diagonal, long, wide Communicative structures I think that the channel could be modelled by a straight line • We need to find if the circle and the line intersect • I think we should choose as coordinate system | □ Whole class ■ Group work □ Pair work □ Individual work | • U1_L4_ALL2.pdf | Formative: • T collects the worksheets and assesses them. • T models language, content and cognition. |
|---|-----|---|---|---|--|------------------|---|
| | | h) Cooperation. | | coordinate system | | | |

| 5 | 20' | a) Developing enquiry and discussion. b) Communication. c) Listening to others. d) Justifying choices, | a) T writes on WB the solutions found by each group and discusses them with the class (especially if they are not all the same). b) T shows on | Skills L S R W Key vocabulary model, coordinate system | ■ Whole class □ Group work □ Pair work □ Individual work | • U1_L4_ALL2.pdf o WB o GeoGebra (on IWB) | Peer and self-assessment. |
|---|-----|--|---|---|--|---|---------------------------|
| | | reasoning and ideas. e) Critical thinking. | the IWB (using GeoGebra) the circle and the line that model the perimeter of the damaged area and the channel respectively, so that Ss can see if they intersect and where. c) Ss that have found a different solutions clarify their reasoning to the rest of the class. The other Ss are asked to find out if that solution is correct and, in case it is not, what is wrong with it. d) T gives some exercises about circle-line intersections for homework. | Communicative structures • Let's use GeoGebra to see who's right. • Are you sure this is the best coordinate system you could choose? • Which mathematical model represents the damaged area? • Which mathematical model represents the channel? • What's wrong with their reasoning? | | | |

Unit number 1 Lesson number 5 Title How to find the equation of a tangent line to a circle.

| Activity | Timing | Learning Outcomes | Activity Procedure | Language | Interaction | Materials | Assessment |
|----------|--------|----------------------|---|--|--|-----------|------------|
| 1 | 10' | | a) T corrects homework if necessary. b) T introduces the objective of the lesson. c) Ss take notes. | Key vocabulary Tangent, secant, external Communicative structures • Today we're going to • Do you have any questions about the homework? | ■ Whole class Group work Pair work Individual work | WB. | |

| 2 | 25' | a) Revising concepts. b) Finding the equation of a tangent line to a circle in one of its points. c) | a) Ss watch an on-line lesson on YouTube that on the one hand helps to revise and on the other hand introduces the topic of the lesson: how to find the equation | Skills L S R W Key vocabulary Gradient, tangent, normal, reciprocal | ■ Whole class □ Group work ■ Pair work □ Individual work | Video available on YouTube: link | Formative: T models and checks language and concepts. |
|---|-----|--|---|--|--|-------------------------------------|---|
| | | Understanding an online lesson. d) Communication. | of a tangent line to a circle. b) T pauses the video when a question is asked and gives Ss time to answer. c) In particular, at the end of the video there are three exercises. At this point, T pauses and Ss try to solve them in pairs. d) After that they continue watching in order to check their solution. | Communicative structures • Do you remember? • Who can tell me? • Find the equation of • What's the relationship between the slopes of these two perpendicular lines? | | | |

3 25' a) Finding the a) T focuses Ss' Skills Whole WB. equation of a attention to an class S R tangent line important point: the W ☐ Group from an method they have used work **Key vocabulary** external point to find the equation of a □ Pair work Delta, quadratic to a circle in tangent line to a circle ☐ Individual equation different ways. in a point P can be work applied only if P belongs b) Communicative Communication. to the circle. b) T asks structures c) Listening to the students to think Suppose that point P others. about the case in which doesn't belong to the P does not belong to the circle,... • Can you find circle (how to find the a tangent line at a equation of a tangent circle passing through from an external point an internal point? • Do to the circle). c) In you think there is plenary, interacting with another method to ...? Ss, T points out two other methods for finding the equation of a tangent line to a circle: 1) setting $\Delta=0$ in the system of the equation of the line and the equation of the circle; 2) setting that the distance between the centre of the circle and the set of all lines passing through the point is equal to the radius. d) T clarifies these two other methods showing examples on the WB.

| 4 | 20' | a) Solving new problems by applying acquired | a) T shows two exercises on the IWB and asks Ss to solve them individually in 20 | Skills L S R W | □ Whole class □ Group work | • U1_L5_ALL1.pdf IWB. | Self- assessment. |
|---|-----|--|--|--|-------------------------------------|-----------------------|----------------------|
| | | knowledge. b) Time managing. c) Using graphs as a mean to | minutes. b) Ss complete them individually. c) T circulates and gives a hint where needed. | Key vocabulary Tangent, secant, external, intersection | □ Pair work ■ Individual work | | |
| | | check own work. | | Communicative structures • Excuse me, I have a doubt • Is it correct if I • Are you sure about that? | | | |

| 5 | 20' | a) Consolidating learning. b) Evaluating own work. c) Listening to the others. d) Communication. | a) T asks two Ss to correct the exercises on the WB. b) The other Ss take notes if necessary, check their solution and interact if they have questions or comments. | Skills L S R W Key vocabulary Tangent, secant, external, intersection | ■ Whole class □ Group work □ Pair work □ Individual work | • U1_L5_ALL1.pdf WB. | Formative: • T elicits cognition and content. • self- assessment. |
|---|-----|--|---|--|--|----------------------|---|
| | | e) Presenting an opinion. | c) T supervises and coordinates the correction, facilitating Ss's participation. d) T asks Ss if it is possible to apply different methods to the same exercise. e) T gives Ss other exercises and problems for homework and provides instructions for the test of next lesson. | Communicative structures • Here I've applied the second method because • Excuse me, I have a question • I did it differently • Do you think we could apply the first method as well? • What's the easiest way? | | | |

Unit number 1 Lesson number 6 Title Test to consolidate learning.

| Activity | Timing | Learning Outcomes | Activity Procedure | Language | Interaction | Materials | Assessment |
|----------|---------------------------------|--|---|---|-----------------------|-------------------|-------------------------------------|
| 1 | 30' | a) Consolidating learning. b) | a) T hands out the tests and asks if all the questions are clear. b) T | Skills L S R W | □ Whole class □ Group | • U1_L6_ALL1.pdf | Formative: T collects the tests and |
| | Revising. c) Critical thinking. | sets a 30-minutes time limit for the test. c) Ss complete the test | Key vocabulary □ Pa | work □ Pair work ■ Individual | | assesses them. | |
| | | | individually. d) Exercise n° 3 has no solution. Ss have to reflect on this point; it is not enough to simply apply knowledge. | Communicative structures • Is everything clear? • You have 30 minutes to complete the test. | work | | |

| 2 | 20' | a) Consolidating knowledge. b) Finding different ways to solve the | a) T corrects the test on the WB, discussing the solutions together with Ss. b) For each exercise T asks Ss to think about different ways to solve | Skills L S R W Key vocabulary See U1_L1_ALL1 | ■ Whole class □ Group work □ Pair work □ Individual | • U1_L6_ALL1.pdf WB. | Self- assessment. |
|---|-----|--|---|--|---|----------------------|----------------------|
| | | same problem. c) Evaluating own work. | it. c) Ss asks for clarifications and take notes if needed. d) After the correction, Ss are asked to self-evaluate. | Communicative structures • Can you think about another way to get to the solution? • Do you find it easier? • Excuse me, why couldn't we simply? • Now that you know all the solutions, give a mark to your own work. | work | | |

Unit number 1 Lesson number 7 Title Relative position of two circles.

| Activity | Timing | Learning Outcomes | Activity Procedure | Language | Interaction | Materials | Assessment |
|----------|--------|---|--|---|--------------------------|-----------|------------|
| 1 | 5' | | a) T introduces | Skills | ■ Whole | | |
| | | objective, learning outcomes and activities of this lesson. | outcomes and | L S R W | class □ Group work | | |
| | | | Key vocabulary relative position, intersection, circles | ☐ Pair work ☐ Individual work | | | |
| | | | | Communicative structures • Today we're going to talk about • We're going to explore the different relative positions of two circles | | | |

| 2 | 15' | a) Understanding the relative positions of two circles. b) Classifying pairs of circles according to their reciprocal position. c) Exploring a | a) T hands out the worksheets, asks Ss to complete them in pairs, distributes one laptop per pair and asks Ss to access them and to download the GeoGebra file U1_L7_ALL2 from a shared folder. a) Ss | Skills L S R W Key vocabulary Externals, secants, eccentric/concentric interiors, internally/externally tangent | □ Whole class □ Group work ■ Pair work □ Individual work | • U1_L7_ALL1.pdf • U1_L7_ALL2.zip One laptop per pair. | Formative: T models language, cognition and concepts. |
|---|-----|--|---|---|--|---|---|
| | | problem using a GeoGebra simulation. d) Formalizing what has been experimented using GeoGebra. e) Cooperating. | complete their task in pairs, also exploring the simulation in GeoGebra. b) T circulates to give hints where necessary. | Communicative structures • First of all two circles can have up to two intersections. • They could be one inside the other • How many different relative positions could we find? • There's another possibility • I've just found another example | | | |

| 3 | 5' | a) Understanding the relative positions of two circles. b) Formalizing what has been experimented using GeoGebra. | a) T asks Ss to share their results and quickly corrects the task. b) Ss can ask questions if they have doubts and interact with T. | Skills | ■ Whole | |
|---|----|---|---|--|---------------------------------------|--|
| | | | | Externals secants | ☐ Group work ☐ Pair work ☐ Individual | |
| | | | | tangent Communicative structures • Did you think of all cases? • Was your classification similar or | | |
| | | | | different from the classification you found on the other side of the worksheet? | | |

| 4 | 40' | a) Finding the intersection points of two circles. b) Comparing different methods for finding the intersection points of two circles and recognizing the easiest. c) Applying acquired a) T forms groups of three Ss and hands out the worksheets for next activity. b) Ss complete them and ask T for clarifications if needed. c) T circulates to facilitate. | | Skills | ☐ Whole • U1_L7_ALL3.pdf class | Formative: T models language, content and cognition. |
|---|-----|--|---|--|--------------------------------|--|
| | | | L S R W Key vocabulary radical axis, substitution, elimination, comparison Communicative structures | ■ Group work □ Pair work □ Individual work | | |
| | | knowledge to new problems and situations. d) Critical thinking. e) Demonstrating a geometrical property using analytic geometry. f) Cooperation. g) Time managing. | | • I'm pretty sure we've to solve the system • In your opinion which method is easier? • I think it's better to use elimination because • Two lines are perpendicular if their slopes are | | |

| 5 | 20' | a) Finding the intersection points of two circles. b) Evaluating the work of oneself and others. c) Critical thinking. d) Communication. | a) T discusses the results with Ss. b) Ss are invited to share their ideas with the rest of the class. c) The proof of last point (the radical axis is perpendicular to the line that connects the two centres of the circle) is particularly interesting and therefore T spends some minutes discussing it and checking if Ss understood it. d) After the correction, T asks Ss to consider the case of external circles. Which geometrical property does the radical axis satisfy in this case? e) T writes on WB Ss' ideas and then formalizes. | Skills L S R W Key vocabulary radical axis, substitution, elimination, comparison | ■ Whole class Group work Pair work Individual work | | Formative: • T elicits content, cognition and language. • Peer and self- assessment |
|---|-----|--|--|---|--|--|---|
| | | | | Communicative structures • Which method did you use to find? Could you tell to the rest of the class how did you proved this property of the radical axis? • What if the circles are externals? What could we say about the radical axis? | | | |

| 6 | 15' | a) Revising acquired knowledge. b) Consolidating | a) The last activity is a competition in three parts. T explains the rules of the game. b) | Skills L S R W Key vocabulary | ■ Whole class Group work Pair work | • U1_L7_ALL4.pdf WB | Formative: T gives a point to the winner(s) of the game |
|---|-----|--|--|--|------------------------------------|------------------------|---|
| | | learning. c) Time managing. | T writes a question (see U1_L7_ALL4) on the WB: Ss should determine the relative position of two circles, knowing some conditions (there are three different sets of conditions and therefore three parts to the game). c) T writes the first set of conditions on WB and Ss work individually as fast as they can. d) The first S that gets the answers calls T, who stops the time. e) | Key vocabulary set, condition, equation Communicative structures • Are you ready for the first set of conditions? • They are internally tangent, correct! • That's right! • Let's move on to the next set of conditions. | □ Pair work ■ Individual work | | the game. |
| | | | If it is correct, they proceed: T writes the second set of conditions on WB and the game starts again. f) If it is not correct, Ss have some more minutes to find the right answers. g) At the end T gives some more exercises for homework. | | | | |

Unit number 1 Lesson number 8 Title Families of circles.

| Activity | Timing | Learning Outcomes | Activity Procedure | Language | Interaction | Materials | Assessment |
|----------|--------|---|--|---|-------------------------------|-----------|------------|
| 1 | 15' | a) Revising knowledge. b) | a) T checks the homework and | Skills | ■ Whole class | | |
| | | Consolidating corrects it if necessary. learning. b) Ss ask for | ☐ Group work | | | | |
| | | | clarifications if needed. c) T asks Ss questions about previous lesson in order to revise knowledge before proceeding. d) T introduces objective | Key vocabulary Externals, secants, eccentric/concentric interiors, internally/externally tangent, family of curves | □ Pair work □ Individual work | | |
| | | | and learning outcomes of this lesson. | Communicative structures • Do you have any questions about the homework? • Do you remember what it's called when two circles have the same centre and different radii? • Today we're going to explore | | | |

| 2 | 25' | a) Working with parametric equations, understanding what they represent. b) Exploring and | a) T hands out the worksheets for the first activity, reads them and asks Ss if the requests are all clear. b) Ss complete the task in pairs. c) T | Skills L S R W Key vocabulary Family of curves, parametric equation | ☐ Whole class ☐ Group work ■ Pair work ☐ Individual work | • U1_L8_ALL1.pdf | Formative: T models language and concepts. |
|---|-----|---|--|---|--|------------------|--|
| | | then analyzing a new mathematical object (a parametric equation) and finding some of its properties. c) Developing reasoning skills. d) Developing enquiry. e) Cooperation. | circulates to facilitate. | Communicative structures • They are concentric circles, aren't they? Excuse me, is it right if I say • They are all circles with centre on | | | |

3 15' a) The ability to a) T asks Ss to share Skills Whole • U1 L8 ALL1.pdf T work with their results. b) T, class encourages WB. S R together with Ss, W ☐ Group peer and parametric equations, corrects the exercises. work self-**Key vocabulary** understanding c) T underlines an □ Pair work assessment. Family of curves, what they important learning ☐ Individual parametric equation represent. b) outcome of this work: work Reflecting on at first Ss might be **Communicative** probably worried t to learning structures face this equation together. c) • Which curves does because this is the first Reflecting on the this equation best approach to time they have to deal represent? • What's the with a parametric an apparently equation of the line you problematic task. equation in this found? • What did you Module. However, after d) Developing think at fist when you trying, they will realize discussion and saw this equation? • that they understand communication. Then you discovered the equation and can that this task was not answer the relative as difficult as you had questions. This means imagined... • What that on the one hand does this experience they should always try teach us? without being discouraged by appearances and on the other hand working together can make an apparently problematic task easier. d) Ss discuss this point with T, evaluating their approach to this "problematic task".

| 4 | 15' | a) Critical thinking. b) Communication. c) Making hypotheses. | a) T hands out the worksheets for the next activity, that is connected with the previous activity. b) This time Ss are prepared to face a | Skills L S R W Key vocabulary Family of circles, intersection points | ☐ Whole class ☐ Group work ■ Pair work ■ Individual work | • U1_L8_ALL2.pdf | |
|---|-----|---|--|--|--|------------------|--|
| | | | parametric equation. Therefore they are asked to work at first individually for 10 minutes, then to share their ideas in pairs. c) T circulates. | Communicative structures • I think that • It seems that the intersection points are the same for each pair of circles of this family. • You're right! • But are you sure that it works for each pair of circles of the family? | | | |

| 5 | 20' | a) Formalizing. b) Understanding the concept of | a) T discuss their results with Ss. b) T confirms and | Skills L S R W | ■ Whole class | • U1_L8_ALL2.pdf WB |
|---|-----|---|--|---|------------------------------------|---------------------|
| | | family of circles and knowing its properties. c) Classification of | formalizes Ss' hypotheses about the "fixed points" of the family of circles in the | Key vocabulary family of circles, central axis | work □ Pair work □ Individual work | |
| | | families of circles. | worksheet. c) T formally introduces the concept of "family of circles" and presents the different kinds of families of circles. d) T is not interested in studying this topic in depth, T's aim is just to tell Ss the main properties of families of circles. e) Ss take notes and ask for clarifications if necessary. | Communicative structures • What's your hypothesis after the investigation? • Let's formalize this concept in a rigorous definition. • There are different kinds of families of circles according to • It could be proved that | | |

| 6 | 10' | a) Consolidating learning. b) Time managing. c) Applying acquired knowledge in a new situation. | a) In order to apply and consolidate what has been learnt, T challenges Ss to individually answer a question shown on the WB. b) The winner of this challenge is the first S who manages to | Key vocabulary Family of circles, concentric, secants, tangent | ■ Whole class Group work Pair work Individual work | • U1_L8_ALL3.pdf WB | Formative: T gives a point to the winner of the game. |
|---|-----|---|---|---|--|---------------------|---|
| | | | answer correctly. c) This answer is then discussed in plenary. d) T gives some more exercises for homework. | Communicative structures • Now I would like you to answer to the following question individually • Correct! Can you explain your reasoning to the rest of the class? | | | |

Unit number1Lesson number9TitleSubsets of the plane.

| Activity | Timing | Learning Outcomes | Activity Procedure | Language | Interaction | Materials | Assessment |
|----------|--------|----------------------|---|---|--|-----------|------------|
| 1 | 10' | | a) T revises briefly what was learnt in | Skills L S R W | ■ Whole class | | |
| | | | the previous lesson. b) T introduces objective, learning outcomes and | Key vocabulary Subset, area, perimeter, intersection | ☐ Group work ☐ Pair work ☐ Individual work | | |
| | | | activities of this lesson. | Communicative structures • Today you're going to represent particular subsets of the plane • You'll find this activity particularly interesting because | | | |

| 2 | 30' | a) Formulating hypotheses and supporting them through examples or counterexamples. b) Graphically representing subsets of the plane that involve circles and lines. c) Interpreting and understanding which points are solutions of inequalities such as x^2+y^2≤1 d) | a) T hands out the worksheets for the first activity and asks Ss to complete them in pairs. b) Ss work in pairs and ask for clarifications if necessary. c) Ss might not understand immediately how to deal with the given subsets of the plane. d) T lets Ss | Key vocabulary Subset, less than or equal to, greater than or equal to, circular crown, half plane Communicative structures Try to understand which subset this is Find some examples in | □ Whole class □ Group work ■ Pair work □ Individual work | • U1_L9_ALL1.pdf | Formative: T models language, cognition and concepts. |
|---|-----|---|---|---|--|------------------|---|
| | | x^2+y^2≤1 d) Critical thinking. e) Cooperation and communication. | plane. d) T lets Ss think about the issue for some minutes without helping them or answering their questions. e) Then T circulates to facilitate. | order to check your hypothesis • I think this is the set of all points that are outside the circle. • Do you think this could be a half plane? | | | |

| 3 | 20' | a) Representing subsets of the plane | a) T asks Ss to share their results | Skills | ■ Whole class | U1_L9_ALL1.pdfU1_L9_ALL2.pdf | Peer and self- |
|---|-----|--|--|--|-------------------------------|---|----------------|
| | | that involve circles and lines. b) | in plenary. b) Each couple of Ss is | L S R W | ☐ Group work | WB. | assessment. |
| | | Listening to others. c) Comparing different approaches. d) Justifying choices. e) Communication. | invited also to explain the cognitive and mental process they went through to get to their | Key vocabulary Less than or equal to, greater than or equal to, subset of the plane, circular crown, half plane | ☐ Pair work ☐ Individual work | | |
| | | | result. c) Ss can now compare their different approaches to the problem and their different ways of reasoning. d) T conducts the discussion and writes on the WB the keywords Ss come up with. e) Then T formalizes what Ss have just discovered drawing on the WB a table similar to the table in U1_L9_ALL2. | Communicative structures • How did you get to this result? • Tell the class about • Comparing these two approaches • While they, the other couple • We thought that this set is the set of all points inside the circle of equation • Then we checked our hypothesis using some examples | | | |

| 4 | 25' | a) Visualizing subsets of the plane | a) T hands out the worksheets for the | Skills | □ Whole class | • U1_L9_ALL3.pdf | T circulates, models and |
|---|-----|---|---|--|--|------------------|--------------------------------|
| | | as intersection of half planes, circles or complement of circles. b) Describing subsets of the plane in the set builder form. c) Being aware of the sets language | second activity, which is, in a way, the opposite of previous activity. b) Since the topic is the same, Ss are asked to work individually at first, | L S R W Key vocabulary subset of the plane, half plane, circular segment, circular sector, boundary, set builder form | □ Group work ■ Pair work ■ Individual work | | elicits content and cognition. |
| | | and being able to use it correctly. d) Creative thinking (seeing and recognizing that the area of a certain subset of the plane can be easily obtained by subtracting the areas of two other known geometrical figures. | and only later to discuss in pairs and compare their solutions. c) Despite the fact that the topic is not new, this second activity requires more awareness and a deep understanding of what has previously been done. d) T circulates and provides support to Ss during the activity, observes and listens to them as they work. | Communicative structures • This is the intersection of two half planes and a circle. • The equation of the circle is • What's the equation of the line? • Here we should consider just the boundary of the circle | | | |

| 5 | 15' | a) Describing subsets of the plane in the set builder form. b) Listening to others. c) Communication and discussion. d) Evaluating the work of oneself and | a) Ss can now share their results with the whole class. b) T encourages reflection and discussion. c) T underlines the difference between | Skills L S R W Key vocabulary Set builder form, half plane, circular segment, circular sector, boundary | ■ Whole class □ Group work □ Pair work □ Individual work | • U1_L9_ALL3.pdf | Peer and self-assessment. |
|---|-----|--|---|--|--|------------------|---------------------------|
| | | others. | subsets n° 1, 2, 3 and subsets n° 4, 5. d) T gives similar exercises for homework. | Communicative structures • What's the difference between subset n° 3 and subset n° 4? • How did you translate this difference in terms of conditions to be satisfied? • How did you determine the area of the circular sector? • I have a different idea | | | |

Unit number 1 Lesson number 10 Title A "complex" problem regarding the circle.

| Activity | Timing | Learning Outcomes | Activity Procedure | Language | Interaction | Materials | Assessment |
|----------|--------|--|---|---|------------------------------------|-------------------|--------------|
| 1 | 10' | a) Understanding | a) T introduces objective, learning | Skills | ■ Whole class | • U1_L10_ALL1.pdf | |
| | | the text and | outcomes and activities | L S R W | ☐ Group | | |
| | | the requests of a "complex" problem. | of this lesson. b) During this last lesson before the final test, Ss are going to deal with a | Key vocabulary to scale, miles, lighthouse, buoy | work □ Pair work □ Individual work | | |
| | | | "complex" problem: problem n° 1 of the state exam in 2015 for Italian schools abroad. c) T forms the groups and hands out the text of the problem. d) T asks a S to read it aloud and clarifies the meaning of new vocabulary and, if necessary, the requests of the problem. | Communicative structures • Today you're going to work in groups on a "complex" problem • You'll also need some physics • Could you please read the text? • Please, ask questions if you do not know the meaning of a word | | | |
| 2 | 45' | a) Applying | a) Ss work in groups. b) Ss can organize the | Skills | | • U1_L10_ALL1.pdf | Formative: T |

acquired knowledge to a complex problem. b) Problem solving. c) Creative thinking: in this problem it is not just a matter of applying what has been studied recently about the circle, but, as in every problem of the state exam, of thinking about all mathematical (and physical) tools you know and understanding what could be useful for this particular situation. (what is the best mathematical model to represent the situation). d) Making

work as they prefer (working together or assigning different tasks to each member of the group according to their abilities and then sharing results). c) Ss can solve requests n° 1, 2, 3 but not n° 4 because they do not have all the necessary mathematical tools yet. T will not tell them this fact: if necessary. T will ask them some questions in order to help them realise this on their own.

L S R W

Key vocabulary

Space, time, distance, velocity, minimum, parabola, vertex

Communicative structures

• How can we organize the work? • I could find the intersections between this line and the circle, while you could... • What's the equation of this circle? • How could we find the minimum? • The equation represents a parabola: the minimum is in the vertex!

- □ Whole class □ Group
- Group work
- □ Pair work□ Individual
- □ Individua work

elicits language, cognition and concepts.

| connections | | | |
|------------------|--|--|--|
| and | | | |
| considering | | | |
| different tools | | | |
| (this task | | | |
| requires a | | | |
| basic | | | |
| knowledge of | | | |
| physics and | | | |
| knowledge of | | | |
| the parabola; | | | |
| the topic Ss | | | |
| studied before | | | |
| this module). e) | | | |
| Organizing the | | | |
| work in a | | | |
| group. f) Time | | | |
| managing. g) | | | |
| Cooperating. | | | |

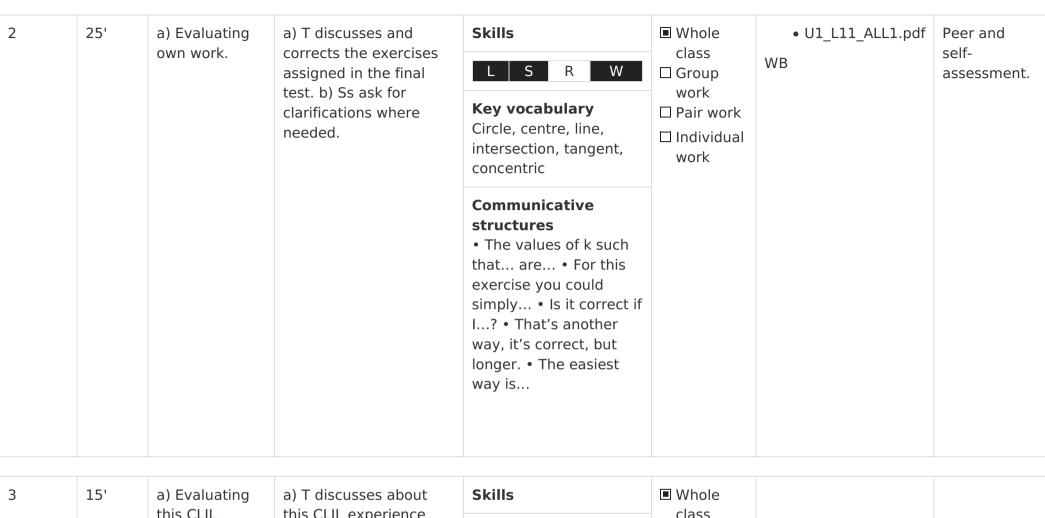
| 3 | a) Analyzing peers' work/Peer assessment. b) Critical thinking. c) Learning from the work of | a) Ss are asked to exchange their work (group 1 gives theirs to group 2 gives theirs it to group 3,). b) T asks Ss to analyze the received work of the other group, | Skills L S R W Key vocabulary Space, time, distance, velocity, minimum, parabola, vertex | ☐ Whole class ☐ Group work ☐ Pair work ☐ Individual work | • U1_L10_ALL1.pdf | Formative: • T models and elicits language, cognition and concepts. • Peer and self- assessment. |
|---|--|---|---|---|-------------------|--|
| | | others. | compare it with their own, in order to formulate some suggestions or corrections to improve it. c) This work is useful also to understand if the own work is correct and/or if it is possible to improve it. d) T circulates, observes and listens to Ss. | Communicative structures • Look at their solution! • Their intersection point is different from ours: let's try to understand who's right! • We forgot to consider • Good, their result is the same as ours! | | |

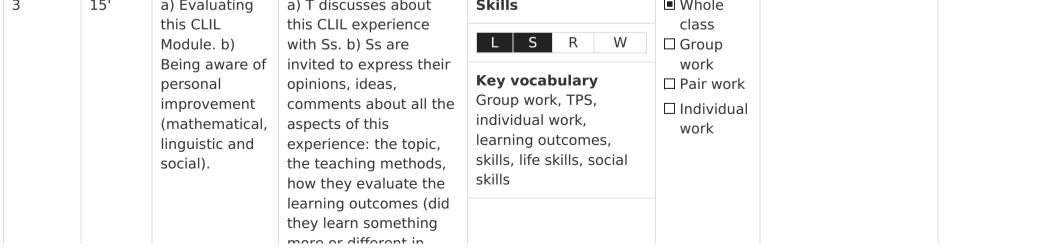
| 4 | 10' | a) Critically analyzing peers' correction. b) Listening to others. | a) Ss return the work to the original group. b) One person per group leaves their group in order to explain the suggestions/corrections that they have made to the other group. c) Ss analyze critically the corrections/suggestions that have been made by the other group. d) T supervises and listens to Ss and to the ambassadors. | Key vocabulary Space, time, distance, velocity, minimum, parabola, vertex Communicative structures • We notice that you forgot to consider • We think that in order to find you need to • I think they're right. • But shouldn't we set the distance between | □ Whole class ■ Group work □ Pair work □ Individual work | • U1_L10_ALL1.pdf | Formative: • T models and elicits language, cognition and concepts. • Peer and self- assessment. |
|---|-----|--|--|---|--|-------------------|--|
|---|-----|--|--|---|--|-------------------|--|

| 5 | a) Evaluating peers' and own work. b) Reflecting on different strategies. c) Reflecting on the importance of group work. d) Understanding what a state exam problem is like and understanding the importance of considering everything you know (every mathematical and physical tool) in order to find an appropriate model and through it a | a) T asks Ss to share their results in plenary. b) In case of doubts, T corrects the problem. c) T invites Ss to reflect on this problem, about how in the state exams all things studied can | Skills L S R W | ■ Whole class □ Group work □ Pair work □ Individual work | Problems and exercises to revise everything that has been studied in this module. | Peer and self-assessment. |
|---|---|--|--|--|---|---------------------------|
| | | | Key vocabulary Space, time, distance, velocity, minimum, parabola, vertex | | | |
| | | of group work. d) Understanding what a state exam problem is like and understanding the importance of considering everything you know (every mathematical and physical tool) in order to find an appropriate model and | be necessary. d) T asks Ss to comment on the activity (did they find it useful to exchange the work with another group? Why?) e) T gives Ss some problems and exercises to revise everything that has been studied in this Module and provides information about the final test. | Communicative structures • As you notice, here you needed to use the kinematic equations you studied in physics • In order to find the minimum distance you need to • For next time, solve these new problems and revise all the exercises and problems we worked on together. • In the final test, you'll | | |

Unit number 1 Lesson number 11 Title Final test.

| Activity | Timing | Learning Outcomes | Activity Procedure | Language | Interaction | Materials | Assessment |
|----------|--|---|---|---|--|---|--|
| 1 | 60' | a) Applying acquired knowledge to new problems and situations. b) Using appropriate terminology. c) | a) T reads the questions of the final test and asks if everything is clear. b) Ss complete the test individually. | Skills L S R W Key vocabulary Circle, centre, line, intersection, tangent, concentric | ☐ Whole class ☐ Group work ☐ Pair work ■ Individual work | class Group work Pair work Individual | Summative: T collects the tests and assesses them. |
| | Analyzing new problems and reasoning critically. | | Communicative structures • Tell me if you do not understand the text. | | | | |





comparison with other Modules in Italian?), if they found it difficult to understand/speak in English, if they enjoyed the activities, which activity they enjoyed the most, suggestions to improve the CLIL experience for next year or Module,...

Communicative structures

- Give me some overall feedback about this experience. Which activity did you enjoy the most? The activity... helped me the most to understand how to find the intersections between...
- Do you think you practiced some important skills that you don't usually practice at school during "normal" lessons? • I found it easy to understand the lessons, whereas speaking was more difficult. • I learnt how to deal with new apparently difficult problems... • Next time I'd like to do more... • In my opinion working in groups was great and useful because...